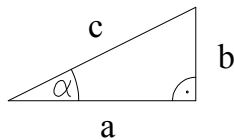


### Vectors, trigonometric functions

What is a vector? size + direction  
 $\underline{v}$  = symbol of a vector (underline)  
 $v$  = length of  $\underline{v}$   
 $\alpha$  = direction of  $\underline{v}$

To add up vectors, we need various trigonometric functions:

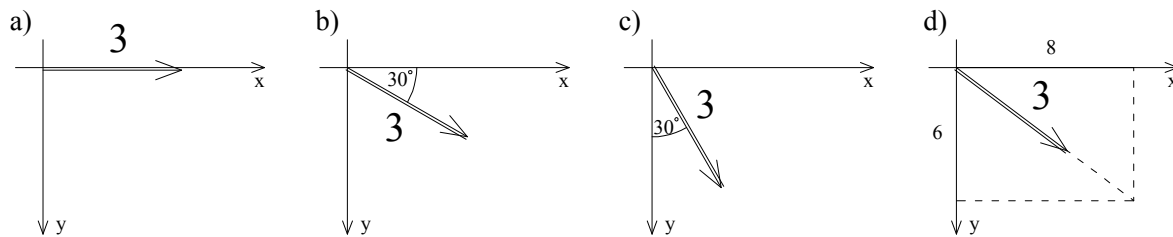


$$\begin{aligned} b / c &= \sin\alpha \\ a / c &= \cos\alpha \\ b / a &= \operatorname{tg}\alpha \\ a / b &= \operatorname{ctg}\alpha \end{aligned}$$

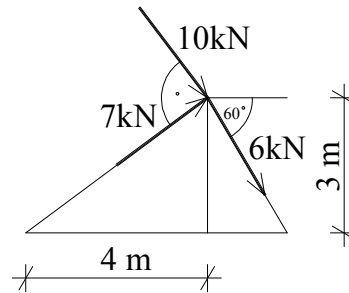
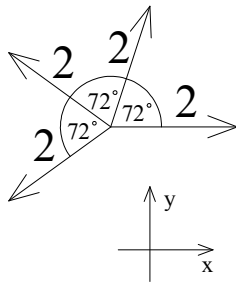
1) Determine the length of the x and y components of the vectors!

Definition: "x component" and "y component" of  $\underline{v}$  are vectors  $\underline{v}_x$  and  $\underline{v}_y$  that are parallel to the x and y axes respectively, and  $\underline{v}_x + \underline{v}_y = \underline{v}$ .

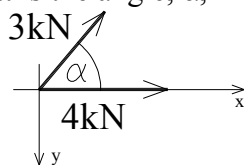
Pythagoras theorem



2) What is the size of the sum of these vectors? What is the direction of the sum?



a) 3) What is the angle,  $\alpha$ , if the size of the sum is:



- a) 7;
- b) 5;
- c) 3;
- d) 1 ?

What is the direction to axis x,  $\beta$ , of the sum in each case?

4) Determine the length of  $\underline{v}$  and  $\underline{w}$  such that the sum of the vector is 0 !

